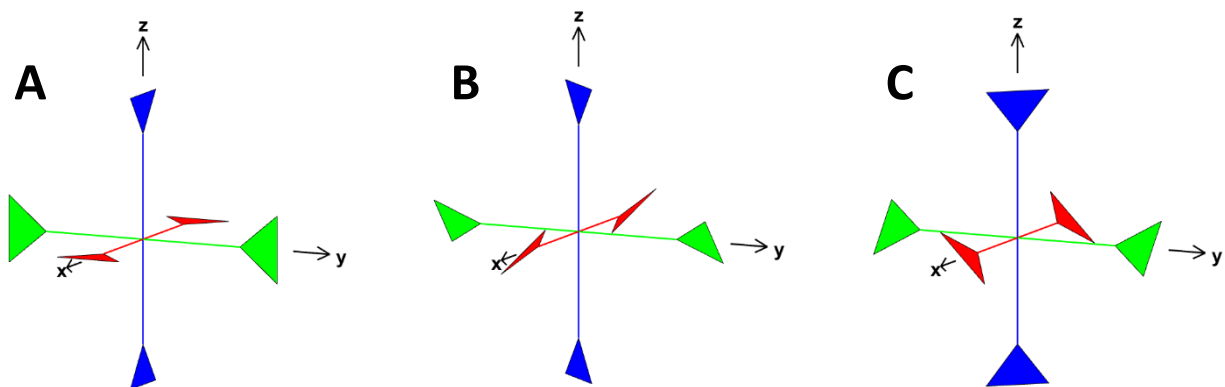


## Problem Set 1

Ch153a – Winter 2021

Due: 8 January, 2021

- 1) Above 13 K, the cesium titanium(III) alum ( $\text{CsTi}(\text{SO}_4)_2 \cdot 12\text{H}_2\text{O}$ ) crystallizes in the cubic space group  $Pa\bar{3}$  with four crystallographically equivalent  $[\text{Ti}(\text{OH}_2)_6]^{3+}$  cations in the unit cell. The  $\text{TiO}_6$  unit adopts a nearly perfect octahedral structure with Ti-O distances of 2.037(1) Å and O-Ti-O angles of 90.37(2)°. Considering just the  $\text{TiO}_6$  units, and assuming  $O_h$  symmetry, what is the ground state term symbol for the  $[\text{Ti}(\text{OH}_2)_6]^{3+}$  cation in this alum?
- 2) The  $\text{OH}_2$  ligands of M(III) in  $\text{CsM}(\text{SO}_4)_2 \cdot 12\text{H}_2\text{O}$  alums (M = Ti, V, Cr, Mn, Fe, Mo, Ru) have a trigonal planar geometry in which the angle between the Ti-O vector and the  $\text{OH}_2$  plane is 0.3(1)°, and *trans*- $\text{OH}_2$  ligand pairs are nearly coplanar. There are three limiting orientations of the  $\text{OH}_2$  planes. In configuration **A**, the  $\text{OH}_2$  ligands on the x-axis lie in the xy plane; the  $\text{OH}_2$  ligands on the y-axis lie in the yz plane; and the  $\text{OH}_2$  ligands on the z-axis lie in the xz plane. In configuration **B**, the  $\text{OH}_2$  ligands on the x-axis are rotated 45° counterclockwise (positive angle) about the x-axis as viewed from the positive x direction; the  $\text{OH}_2$  ligands on the y-axis are rotated 45° counterclockwise (positive angle) about the y-axis as viewed from the positive y direction; and the  $\text{OH}_2$  ligands on the z-axis are rotated 45° counterclockwise (positive angle) about the z-axis as viewed from the positive z direction. In configuration **C**, the  $\text{OH}_2$  ligands on the x-axis are rotated 45° clockwise (negative angle) about the x-axis as viewed from the positive x direction; the  $\text{OH}_2$  ligands on the y-axis are rotated 45° clockwise (negative angle) about the y-axis as viewed from the positive y direction; and the  $\text{OH}_2$  ligands on the z-axis are rotated 45° clockwise (negative angle) about the z-axis as viewed from the positive z direction. MATLAB \*.fig files of the three configurations are posted on the course website ([https://www.bilrc.caltech.edu/Ch153a\\_2021/Ch153.html](https://www.bilrc.caltech.edu/Ch153a_2021/Ch153.html)). You might find it easier to visualize the structures if you view these files in MATLAB.



- a) What are the point groups of configurations **A**, **B**, and **C**?
- b) Give the ground state term for a  $[\text{Ti}(\text{OH}_2)_6]^{3+}$  cation in each configuration (neglecting spin-orbit coupling). Explain each answer on the basis of a simple ligand-field orbital diagram.
- c) Draw a qualitative correlation diagram showing the energies of the lowest states in  $[\text{Ti}(\text{OH}_2)_6]^{3+}$  as the  $\text{OH}_2$  rotation angle increases from  $-\pi/4$  to  $+\pi/4$  (neglecting spin-orbit coupling).
- d) The rotation angle of the  $\text{OH}_2$  plane in  $\text{CsTi}(\text{SO}_4)_2 \cdot 12\text{H}_2\text{O}$  is  $-20.4(1)^\circ$ . Identify the point group for this configuration and predict the ground state term symbol for the  $[\text{Ti}(\text{OH}_2)_6]^{3+}$  cation in this alum (neglecting spin-orbit coupling).

- e) In the  $\text{CsM}(\text{SO}_4)_2 \cdot 12\text{H}_2\text{O}$  ( $\text{M} = \text{Co}, \text{Rh}, \text{Ir}$ ) alums, the  $\text{OH}_2$  ligands adopt a pyramidal geometry rather than trigonal planar. Suggest an explanation for the difference on the basis of the electronic structures of the  $\text{M}(\text{III})$ -aquo ions.